



## 3D numerical study on shell side heat transfer and flow characteristics of rod-baffle heat exchangers with spirally corrugated tubes



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### ABSTRACT

This article presents a numerical simulation of the shell side flow in rod-baffle heat exchangers with spirally corrugated tubes (RBHXsSCT). Results are compared with those in rod-baffle heat exchanger with plain tubes (RBHX). Simulation is conducted to improve the thermo-hydraulic performance in longitudinal flow heat exchangers and to obtain an understanding of the physical behavior of thermal and fluid flow in the RBHXsSCT with Reynolds number ranging from 6000 to 18,000. Simulation results show that the Nusselt number in RBHXsSCT with one-start spirally corrugated tubes can be 1.2 times that in RBHX when the Reynolds number is 18,000. The heat transfer quantities in the RBHXsSCT with one-start, two-start, three-start, and four-start spirally corrugated tubes are 104.6%, 105.4%, 106.7%, and 109.6%, respectively, higher than that in RBHX. The pressure drop in RBHX is 1.21, 1.16, 1.12, and 1.08 times that in RBHXsSCT with one-start, two-start, three-start, and four-start spirally corrugated tubes, respectively. The RBHXsSCT with one-start spirally corrugated tubes can achieve an efficiency evaluate coefficient of 1.35. Physical quantity synergy analysis is performed to investigate heat transfer and flow resistance performance. Results verify the synergy regulation among the physical quantities of fluid particle in the flow field of the convective.

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### 1. Introduction

Shell-and-tube heat exchangers (STHXs) are extensively used in petroleum refining, chemical engineering, and power generation, among others [1]. The fluid flow in STHXs can be divided into tube side flow and shell side flow. A large amount of heat-transfer enhancement techniques, such as rectangular tubes and tube inserts [2–11], have been developed and applied in the tube side of the STHXs to save energy. Meanwhile, the performance of the shell side is mainly dependent on the flow status in STHXs. The heat transfer rate is relatively high in cross flow heat exchangers, such as the segmental-baffle shell-tube heat exchangers [12–20]. However, the pressure drop and the “dead” flow region are extremely large, and harmful vibrations are violent. The longitudinal flow heat exchangers have the following advantages compared with the cross flow heat exchangers: (1) considerable reduction of the pressure drop and the pump power loss in the shell sides; (2) avoidance of the vibrations and security enhancement of heat exchangers; (3) decrease of “dead” flow regions and generation of fouling and corrosion [1]. Therefore, as typical longitudinal flow heat

exchangers, the rod-baffle heat exchangers (RBHXs), which were originally proposed in the 1970s by Phillips Petroleum Company [21–23], have been extensively studied by researchers because of the above mentioned advantages.

Smyth [24] conducted an experimental study on RBHXs. The results showed that in the RBHXs, the heat transfer coefficients slightly increased, and the pressure loss significantly decreased compared with the traditional STHXs, leading to reduced cost of exchangers and in some instances smaller exchangers. Ma et al. [25] analyzed the flow and heat transfer characteristics on the combinations of rod baffle with different types and distances by numerical simulation on the basis of RBHXs. The simulation results indicated that the rod baffle type of ellipse as well as the rod baffle distance of 120 mm showed the best performance. Ma et al. [26] designed a new type of RBHX, which has variable sections to optimize the heat exchanger. The results indicated that the comprehensive performance of the variable section RBHX increased by 13%–14% than the uniform section RBHX. Dong et al. [27] adopted a unit duct model to analyze the influence of the rod baffle on the flow of the shell side and to present the status of turbulent flow and heat transfer in the shell side of the STHX with rod baffle. The simulation results showed that the rod baffles placed vertically and horizontally in the unit duct continuously sheared

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and comminuted the streamlines of the flow when the fluid crosses over the rod-baffles, change the fluid flow directions, and result in the disruption of the continuity and stability of the fluid. Wang [28] proposed and investigated a new type of RBHX with thick and thin rods on the basis of the principle of heat transfer enhancement in the core flow [29]. The results presented that with the combined structure. The heat transfer presented no significant degradation, but the flow resistance can be reduced; thus significantly improving the overall performance.

From the foregoing reviews, we found that few studies focused on changing the types of heat exchanger tubes in RBHX to improve the thermal-hydraulic characteristics of the shell side. In this paper, we put forward the RBHX with spirally corrugated tubes (RBHXsSCT) aiming at improving the overall thermal performance of the shell sides compared with the RBHXs. The numerical simulation method is adopted to visualize the flow region and to predict the thermal-hydraulic performance because the numerical simulation is cheaper and more time-saving compared with the experimental study [30–34]. The 3D numerical simulations with whole models of RBHXsSCT and RBHXs are presented to investigate the heat transfer performances and flow resistance characteristics on the shell side by using the commercial software of FLUNET 14.0 with grid systems generated by ICFEM-CFD. The principle of physical quantity synergy [35–38] is used to discuss the thermal-hydraulic performance of RBHXsSCT.

## 2. Model for whole heat exchanger simulation

### 2.1. Computational model

The computational models of RBHXsSCT and RBHX are shown in Fig. 1, and the numerical simulation is conducted only on the shell side of the heat exchangers. The geometry parameters are listed in Table 1. As shown in Fig. 1 21 heat exchanger tubes are present in each heat exchanger and are in square arrangement. Water is selected as the working fluid.

The following assumptions are made to simplify the numerical simulations: (1) the thermal-physical properties of fluid such as  $\rho$ ,  $\mu$ ,  $c_p$ ,  $\lambda$  are constant; (2) fluid is incompressible, isotropic, and continuous; (3) the effect of gravity is negligible; (4) the flow state is steady.

### 2.2. Numerical simulation method

The general control equation for convective heat transfer is expressed as follows:

$$\text{div}(\rho U \phi) = \frac{\partial}{\partial x} \left( \Gamma \frac{\partial \phi}{\partial x} \right) + \frac{\partial}{\partial y} \left( \Gamma \frac{\partial \phi}{\partial y} \right) + \frac{\partial}{\partial z} \left( \Gamma \frac{\partial \phi}{\partial z} \right) \quad (1)$$

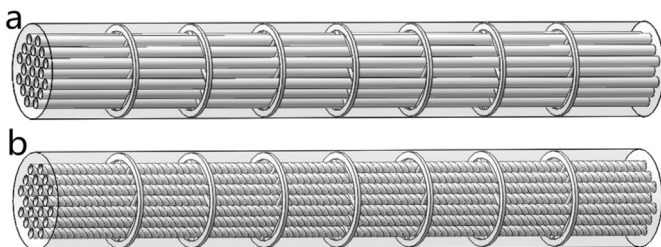


Fig. 1. The model of different heat exchangers. (a) Rod-baffle heat exchanger with plain tubes. (b) Rod-baffle heat exchanger with spirally corrugated tubes.

Table 1  
The geometry parameters of whole model.

Item	Values
<i>Shell-side parameters</i>	
$D$ (mm)	144
Shell-side length (mm)	1000
<i>Rod parameters</i>	
$p_r$ (mm)	5.5
Rod pitch in each baffle (mm)	22
<i>Baffle parameters</i>	
Thickness (mm)	5
Baffle pitch (mm)	120
<i>Spirally corrugated tube parameters</i>	
$d_s$ (mm)	16
Groove depth (mm)	3
Start numbers	1–4
<i>Plain tube parameters</i>	
$d_0$ (mm)	16

where  $\rho$  is the fluid density;  $U$  is fluid velocity vector;  $\Gamma$  is the generalized diffusion coefficient. For continuity equation,  $\phi = 1$ ; for momentum equation,  $\phi$  is velocity vector; and for energy equation,  $\phi = T$ .

The standard  $k-\epsilon$  two-equation model is adopted for the turbulent region, and the two equations are expressed as follows:

$$\frac{\partial(\rho U_i k)}{\partial x_i} = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + G_k + G_b - \rho \epsilon - Y_M + S_k \quad (2)$$

$$\frac{\partial(\rho U_i \epsilon)}{\partial x_i} = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_\epsilon} \right) \frac{\partial \epsilon}{\partial x_j} \right] + C_{1\epsilon} \frac{\epsilon}{k} \left( G_k + C_{3\epsilon} G_b \right) - C_{2\epsilon} \rho \frac{\epsilon^2}{k} + S_\epsilon \quad (3)$$

where  $k$  is the turbulent kinetic energy;  $\epsilon$  is the turbulent dissipation rate;  $G_k$  is the producing item of  $k$  engendered by the average velocity gradient;  $G_b$  is the producing item of  $k$  engendered by buoyancy;  $Y_M$  is the contribution term from turbulent pulse expansion;  $C_{1\epsilon}$ ,  $C_{2\epsilon}$ ,  $C_{3\epsilon}$  are empirical constants;  $\sigma_k$  and  $\sigma_\epsilon$  are Prandtl numbers corresponding to  $k$  and  $\epsilon$ ;  $S_k$  and  $S_\epsilon$  are user-defined source terms.

We then present the boundary conditions. The non-slip boundary condition is applied on all solid surfaces. The standard wall function method is used to simulate flow in the near-wall region. The surfaces of solid regions, rod-baffles, and inner wall of the shell side are set as adiabatic because the heat exchangers are well insulated and the heat loss to surroundings is neglected. The velocity inlet and outflow boundary condition are applied for the inlet and outlet, respectively, because fluid is incompressible. The temperatures of the tube wall and inlet fluid are set as constant, which are 330 and 300 K, respectively. The shell wall and rod-baffle surface are set as adiabatic. The finite volume method and the second-order upwind difference scheme are applied, and the SIMPLEC algorithm is adopted for the coupling between pressure and velocity field. The second-order upwind difference scheme is applied for energy and momentum computation, and the standard

Table 2  
Thermo-physical properties of water.

Parameter	Value
$c_p$ (J/kg K)	4182
$\mu$ (kg/m s)	0.001003
$\rho$ (kg/m <sup>3</sup> )	998.2
$\lambda$ (W/m K)	0.6

difference scheme is used for pressure computation. Water is set as working fluid, and the parameters are given in Table 2.

The 3D grid system was generated by using the commercial software ICEM CFD14.0 on the basis of the 3D geometry created in a commercial CAD program. The computational domain is discretized with unstructured tetrahedral elements, and the regions adjacent to the tubes and the rods are meshed better to meet the requirement of the wall function method. The meshes of the computational model are shown in Fig. 2. Grid independence tests are carried out to ensure that the grid independent solution can be obtained. The results of the grids independent test are shown in Table 3. From the test values of the Nusselt numbers and the pressure drop obtained by the four grid systems, the  $3.6 \times 10^7$  grid system is found to be dense enough to result in grid-independent solutions. Accordingly, the grid system with  $3.6 \times 10^7$  grids is employed to perform the following calculations, and the present numerical predictions have reasonable accuracy. The commercial software Fluent 14.0 is adopted for computational fluid dynamics method, and all numerical simulations are performed on workstations with 20 dual-core CPUs and 240 GB RAM. Every simulation case takes 24 h to obtain the converged solutions approximately.

The paper [40] provides the comparisons of shell-side whole modeling in RBHXs approach on predicting heat transfer and pressure drop with experimental method. In this paper, the maximum discrepancies are about 10.8% for Nusselt number and 12.4% for pressure drop. Therefore it is decided that the whole modeling approach has a high precision on predicting thermal-hydraulic performance.

### 2.3. Data reduction

The Reynolds number of the shell side is expressed as follows:

$$\text{Re} = \frac{\rho u D_e}{\mu} \quad (4)$$

where  $u$  is the inlet average velocity of the shell side;  $\rho$  is the fluid density;  $\mu$  is the coefficient of dynamic viscosity;  $D_e$  is the equivalent diameter, which is expressed as follows:

$$D_{e(\text{RBHX})} = \frac{4A_0}{P_0} = \frac{\pi \cdot D^2 - \pi \cdot n \cdot d_0^2}{\pi \cdot D + \pi \cdot n \cdot d_0} \quad (5)$$

$$D_{e(\text{RBHXsCT})} = \frac{4A_s}{P_s} = \frac{\pi \cdot D^2 - 4 \cdot n \cdot a_{\text{sct}}}{\pi \cdot D + n \cdot p_{\text{sct}}} \quad (6)$$

Here,  $D_{e(\text{RBHX})}$  and  $D_{e(\text{RBHXsCT})}$  are the equivalent diameter of RBHX and RBHXsCT;  $A_0$  and  $A_s$  are the sectional area of RBHX and RBHXsCT;  $P_0$  and  $P_s$  are the sectional wetting perimeter of RBHX

**Table 3**  
Influence of the grid numbers on the computed result.

Grid number	$\Delta \text{Nu}$	$\Delta p$
$9.3 \times 10^6$ to $2.9 \times 10^7$	17%	11%
$2.9 \times 10^7$ to $3.6 \times 10^7$	4.8%	3.9%
$3.6 \times 10^7$ to $4.3 \times 10^7$	2.2%	2.8%

and RBHXsCT;  $a_{\text{sct}}$  is the sectional area of the spirally corrugated tube in RBHXsCT;  $p_{\text{sct}}$  is the perimeter of the spirally corrugated tube;  $n$  is the number of tubes.

For the readers' convenience, the major equations on heat transfer are shown as follows:

$$Q = M \cdot c_p \cdot (t_{\text{out}} - t_{\text{in}}) \quad (7)$$

$$h = \frac{Q}{S \cdot \Delta t_m} \quad (8)$$

$$\Delta t_m = \frac{\Delta t_{\text{max}} - \Delta t_{\text{min}}}{\ln(\Delta t_{\text{max}}/\Delta t_{\text{min}})} \quad (9)$$

$$\Delta t_{\text{max}} = t_{\text{wall}} - t_{\text{in}} \quad (10)$$

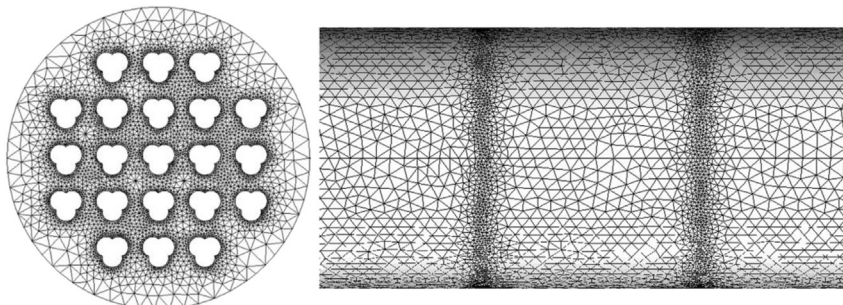
$$\Delta t_{\text{min}} = t_{\text{wall}} - t_{\text{out}} \quad (11)$$

$$\text{Nu} = \frac{h \cdot D_e}{\lambda} \quad (12)$$

## 3. Simulation results and discussions for the models of RBHXsCT and RBHX

### 3.1. Flow structure

The vector plots of velocity, where the fluid flows across the rods in RBHX and RBHXsCT, are shown in Figs. 3 and 4. As seen in Fig. 3, the vortices are generated in the zones where the fluid flows across the rods. Simultaneously, a number of vortices can be observed near the tube wall. These vortices enhance the heat transfer rate between the fluid and the tubes. This phenomenon is considered the heat transfer enhancement mechanism in RBHX. However, in Fig. 4, we can observe that little vortices were generated when the fluid flows across the rods. In Fig. 5 the path lines of fluid which flow between Rod-baffles in different heat exchangers were given. It can be observed that the path lines between Rod-baffles in RBHX are almost parallel with each other. Meanwhile, the path lines between Rod-baffles in RBHXsCT are much more curved than those in RBHX due to the influence by the spirally corrugated tubes. That is to say, between the Rod-baffles, the fluid in RBHX flow along the



**Fig. 2.** The mesh of Rod-baffle heat exchanger.

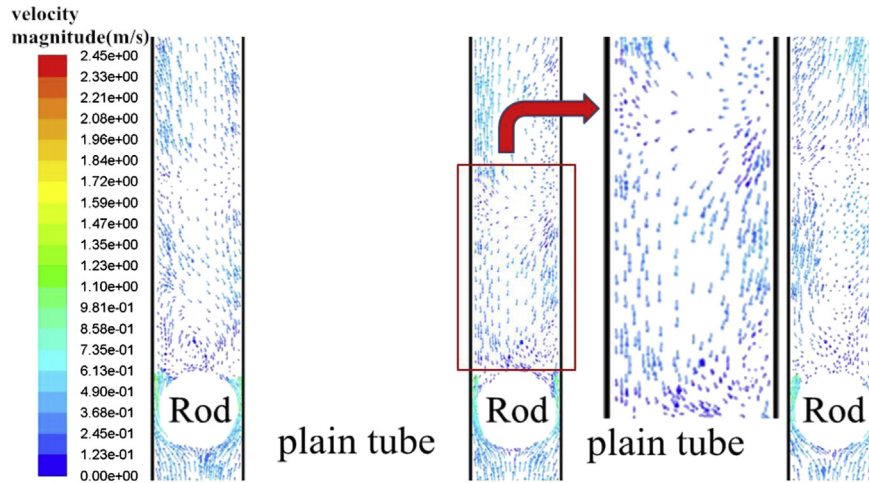


Fig. 3. The velocity vector in Rod-baffle heat exchanger with plain tubes ( $Re = 18,000$ ).

plain tubes, and the fluid in RBHXsCT is led by the spiral corrugated tubes to flow against the tube wall. The different flow structures between the RBXHSCT and RBHX result in different thermo-hydraulic performances in RBXHSCT and RBHX, which will be discussed in detail in the following sections.

### 3.2. Heat transfer

In Fig. 6, the heat transfer performance in terms of the Nusselt numbers of the RBHXsCT with spirally corrugated tubes are compared with those in RBHX. From this figure, we can see that for each Reynolds number, the Nusselt number increases as the start number of the RBXHSCT decreases. The results show that the Nusselt number in RBHXsCT with one-start spirally corrugated tubes can achieve 287.7, which is 1.2 times than that in RBHX when the Reynolds number is 18,000. Meanwhile, the Nusselt number in RBHX are between those in RBHXsCT with three-start and four-start spirally corrugated tubes. This phenomenon is caused by the fact that the heat transfer enhancement mechanism in RBHX is caused by the vortices generated near the tube wall when the fluid flows across the rod. In the heat transfer enhancement mechanism

in RBHXsCT, which is different from that in RBHX, fluid is led by the spiral flow channels of the spirally corrugated tubes to flow against the tube wall. Fig. 7 shows the plots of velocity fields on cross sections in RBHXsCT with different start number spirally corrugated tubes when the Reynolds number is 18,000. From this figure, we can observe that as the start number decreases, the warm area becomes larger and the warm degree becomes deeper. Meanwhile, the “red zones” are closer to the tube walls as the start number decreases. That is to say, the velocity gradient becomes larger near the walls. This demonstrate that the lower the start number of the spirally corrugated tubes, the more intense the disturbance to the fluid by the tubes. Therefore, the heat transfer performance in RBHXsCT with one-start spirally corrugated tubes is better than that in other styles of RBHXsCT and RBHX. The disturbance to the fluid by the tubes is relatively weak in RBHXsCT with four-start spirally corrugated tubes. Thus, the Nusselt numbers in RBHXsCT with four-start spirally corrugated tubes are the least among all the heat exchangers.

Fig. 8 shows the heat transfer quantities in RBHXsCT and RBHX. Although the Nusselt numbers in RBHXsCT with four-start spirally corrugated tubes are smaller than those in other heat exchangers,

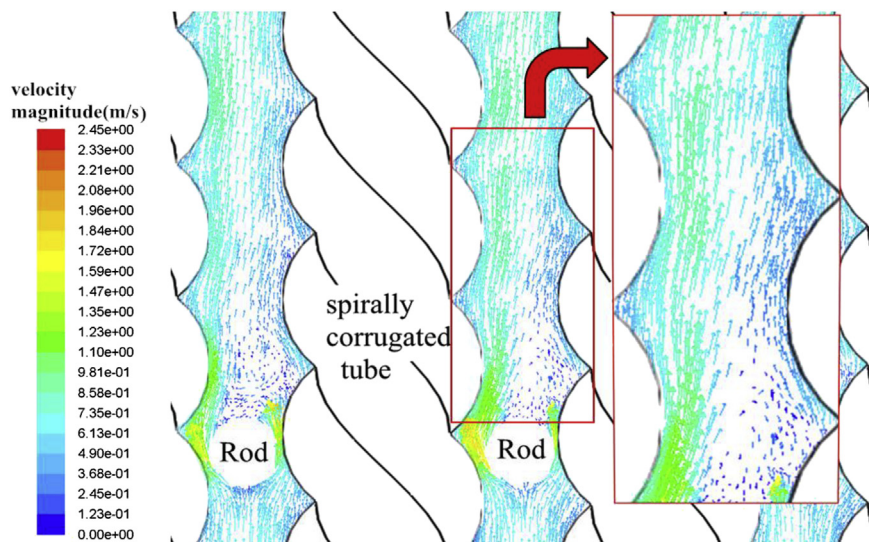


Fig. 4. The velocity vector in Rod-baffle heat exchanger with spirally corrugated tubes ( $Re = 18,000$ ).

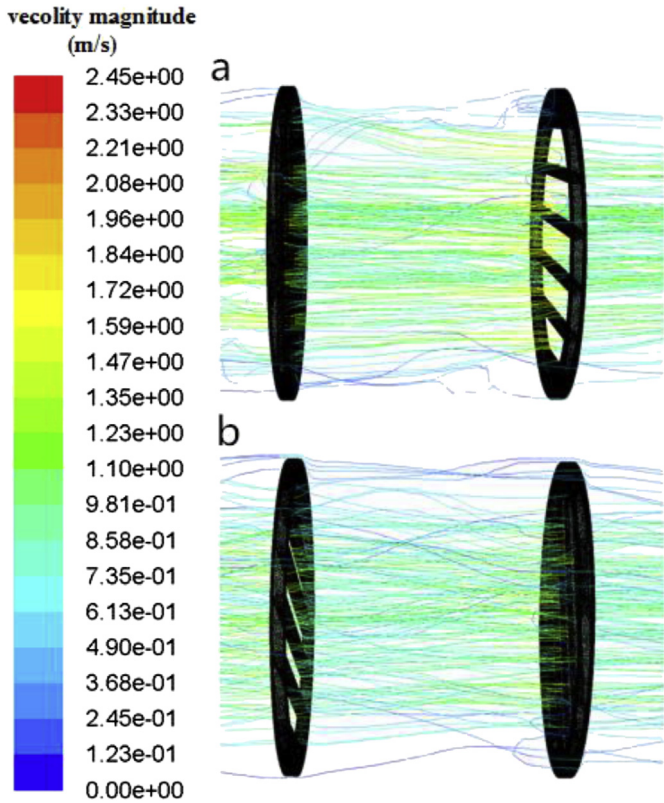


Fig. 5. The path lines in different heat exchangers ( $Re = 18,000$ ). (a) The path lines in RBHX. (b) The path lines in RBHXsCT with spirally corrugated tubes.

RBHXsCT with four-start spirally corrugated tubes has the largest heat transfer quantities among all heat exchangers. The heat transfer quantities in RBHXsCT are all larger than those in RBHX. The results show that the heat transfer quantities in the RBHXsCT with one-start, two-start, three-start, and four-start spirally corrugated tubes are 104.6%, 105.4%, 106.7%, and 109.6%, respectively, higher than that in RBHX. This finding can be attributed to the fact that the higher the start number of the RBHXsCT, the more heat transfer area in the heat exchangers. Although the heat transfer rates are smaller in RBHXsCT with corrugated tubes with more start number, the total heat transfer quantities in these heat exchangers are larger than those in RBHX.

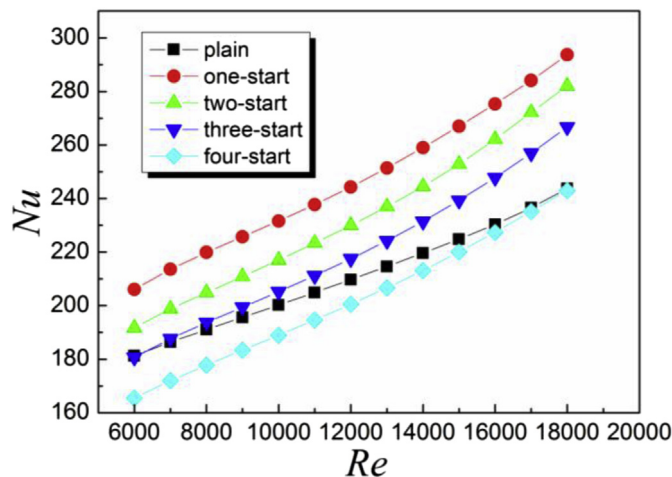


Fig. 6. Variation of Nusselt number with Reynolds number for RBHX and RBHXsCT.

To illustrate the different thermal performances between the RBHX and RBHXsCT with one-start spirally corrugated tubes, we take a section every 200 mm in those heat exchangers mentioned above and present the temperature field plots of these sections in Fig. 9 when the Reynolds number is 18,000. It is clearly observed that, as the flow develops, the warm areas and temperature levels of temperature fields in RBHXsCT with one-start spirally corrugated tubes are larger than those in RBHX. It demonstrates that in RBHXsCT with one-start spirally corrugated tubes, the heat from heat exchanger tubes transfer into the shell side fluid more easily than that in RBHX which agrees well with the phenomena shown in Fig. 6.

### 3.3. Pressure drop

Fig. 10 shows the variation of pressure drops with Reynolds number for RBHX and RBHXsCT. In this figure, the pressure drop in RBHX is larger than that in RBHXsCT. Furthermore, for each Reynolds number, the lower the start number of the spirally corrugated tubes in RBHXsCT, the less the pressure drop. The pressure drop in RBHX is 1.21, 1.16, 1.12, and 1.08 times that in RBHXsCT with one-start, two-start, three-start, and four-start spirally corrugated tubes, respectively. In RBHX, the vortices generated near the tube wall lead to large local resistance loss. However, few vortices are generated in RBHXsCT; thus, the pressure losses mainly come from the on-way resistance loss, which is less than the local resistance loss. The higher the start numbers of the RBHXsCT, the more spiral flow channels are present in RBHXsCT, and the more disturbance occurs to the fluid. Therefore, the pressure drop in RBHXsCT with one-start spirally corrugated tube is less than that of other RBHXsCT and RBHX.

Fig. 11 shows the plots of pressure fields in RBHX and RBHXsCT with one-start spirally corrugated tubes which is set as an example when the Reynolds number is 18,000. It is shown that the pressure distributions on the sections of RBHXsCT with one-start spirally corrugated tubes are very homogenous as those in RBHX. Thus, the induced vibration can be prevented effectively in RBHXsCT which improve the security and reliability of the heat exchangers.

### 3.4. The overall heat transfer performance

Liu et al. [38] presented the efficiency evaluation coefficient (EEC) in heat transfer process on the basis of the power consumption to describe the heat transfer enhancement degree, which is defined as follows:

$$EEC = \frac{Q/Q_0}{P/P_0}, \tag{13}$$

where  $Q$  and  $P$  are the quantity of heat transfer and power consumption in objective equipment, respectively;  $Q_0$  and  $P_0$  are the quantity of heat transfer and power consumption in the comparable equipment, respectively. In this paper, the objective equipment is the RBHXsCT, and the comparable equipment is the RBHX. The power consumption  $P$  and  $P_0$  are calculated as in Eqs. (14) and (15):

$$P = v_s \cdot \Delta p_s, \tag{14}$$

$$P_0 = v_0 \cdot \Delta p_0, \tag{15}$$

where  $v_s$  and  $v_0$  are the volume flow rate of RBHXsCT and RBHX, respectively;  $\Delta p_s$  and  $\Delta p_0$  are the pressure drops in RBHXsCT and RBHX, respectively.

According to the Eqs. (13)–(15), it is clearly that EEC is larger than 1 or close to 1, is ideal and applicable for energy-saving purpose as the ratio of heat transfer enhancement is larger than the

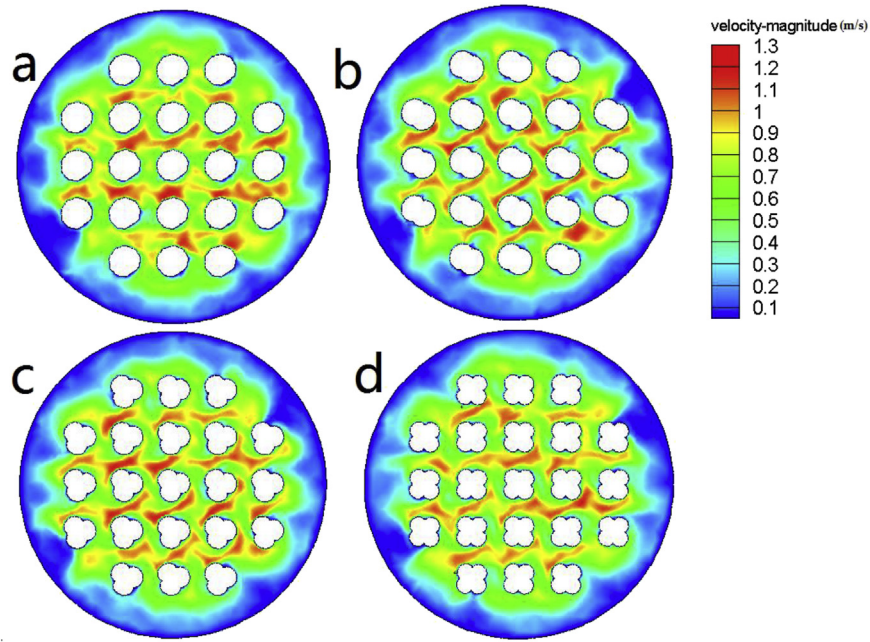


Fig. 7. The plots of velocity fields on cross sections in RBHXsSCT with different start number spirally corrugated tubes (Re = 18000). (a) One-start spirally corrugated tubes. (b) Two-start spirally corrugated tubes. (c) Three-start spirally corrugated tubes. (d) Four-start spirally corrugated tubes.

ratio of power consumption increase. Fig. 12 shows the EEC values in RBHXsSCT with different start numbers. From this picture, we can find that all the EEC values in RBHXsSCT are larger than 1. Thus, compared with the RBHX, the profit (quantity of heat transfer) increase rate is larger than the cost (power consumption) increase rate in RBHXsSCT. This is because the spirally corrugated tubes in heat exchangers influence the shell side fluid, and change the flow condition, which improve the overall thermal performance. The EEC value in RBHXsSCT with one-start spirally corrugated tubes can archive 1.35 when the Reynolds number is 18,000, thus making this heat exchanger promising to be widely applied in various industries.

3.5. Physical quantity synergy analysis

Guo [39–41] investigated the physical mechanism of convective heat transfer and proposed field synergy principle to enhance heat

transfer, considering the evaluation of convective heat transfer is related to the synergy of velocity and temperature field. Liu et al. [35–37] proved multi-field physical quantity synergy for convective heat transfer by introducing more synergy angles on the basis of velocity field, temperature field, and pressure field and by revealing the fundamental nature of heat transfer enhancement and pressure reduction. The physical nature of enhancing heat transfer and reducing flow resistance, which is directly associated with synergy angles  $\beta$  and  $\theta$ , is also explained.

The synergy angle between the velocity vector  $\vec{U}$  and temperature gradient  $\nabla T$  of a fluid particle  $M$  in the flow field can be written as

$$\beta = \arccos \frac{\vec{U} \cdot \nabla T}{|\vec{U}| |\nabla T|} \tag{16}$$

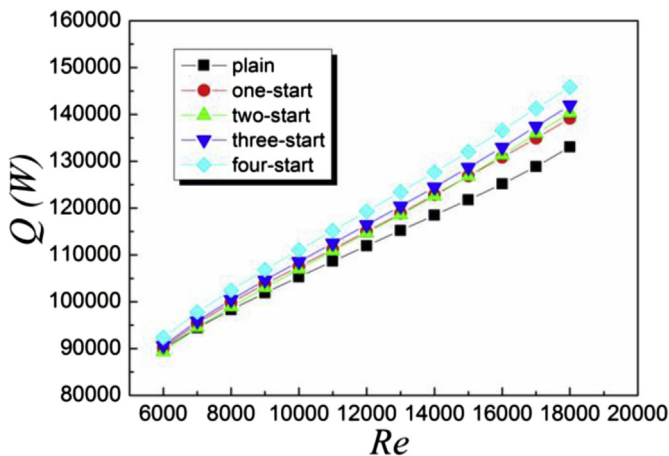


Fig. 8. Variation of the heat transfer quantities with Reynolds number for RBHX and RBHXsSCT.

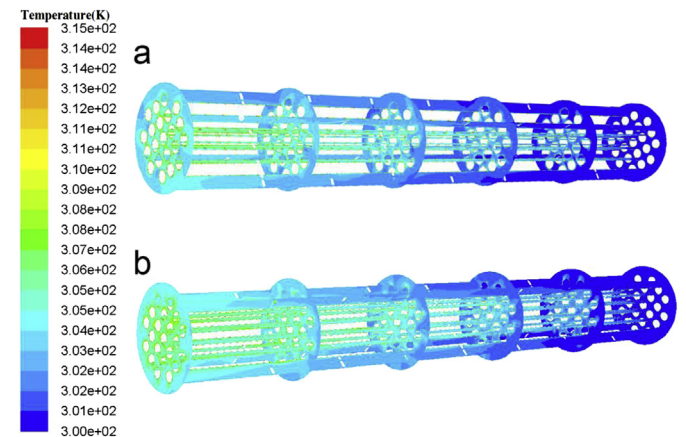


Fig. 9. The plots of temperature fields in different heat exchangers. (a) The plots of temperature fields in RBHX. (b) The plots of temperature fields in RBHXsSCT with one-start spirally corrugated tubes.

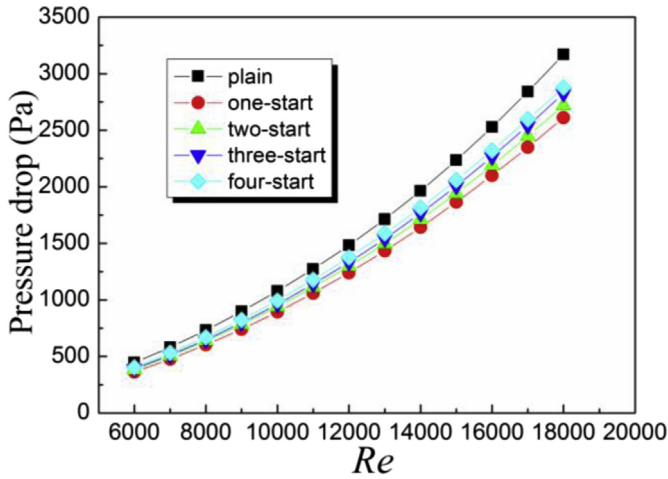


Fig. 10. Variation of pressure drop with Reynolds number for RBHX and RBHXsSCT.

The synergy angle between the velocity vector  $\vec{U}$  and pressure gradient  $\nabla p$  of a fluid particle  $M$  in the flow field can be written as

$$\theta = \arccos \frac{\vec{U} \cdot \nabla p}{|\vec{U}| |\nabla p|} \quad (17)$$

Fig. 13 shows the average synergy angle  $\beta$  for RBHX and RBHXsSCT with different start numbers of the spirally corrugated tubes. As shown in the figure, the average synergy angle  $\beta$  between fluid velocity  $\vec{U}$  and temperature gradient  $\nabla T$  decrease as the start number decreases in the RBHXsSCT at the same Reynolds number, and the  $\beta$  values in RBHX are between those in RBHXsSCT with three-start and four-start spirally corrugated tubes. By observing Fig. 13 we can conclude that the smaller the average synergy angle  $\beta$ , the higher the heat transfer rate is, which is in accordance with the conclusions of [36] and [41].

Fig. 14 shows the average synergy angle  $\theta$  for RBHX and RBHXsSCT with different start numbers of the spirally corrugated tubes. As shown in the picture, the average synergy angle  $\theta$  between fluid velocity  $\vec{U}$  and pressure  $\nabla p$  decreases as the start number decreases in the RBHXsSCT at the same Reynolds number, and the  $\theta$  values in RBHX are the biggest among all heat exchangers.

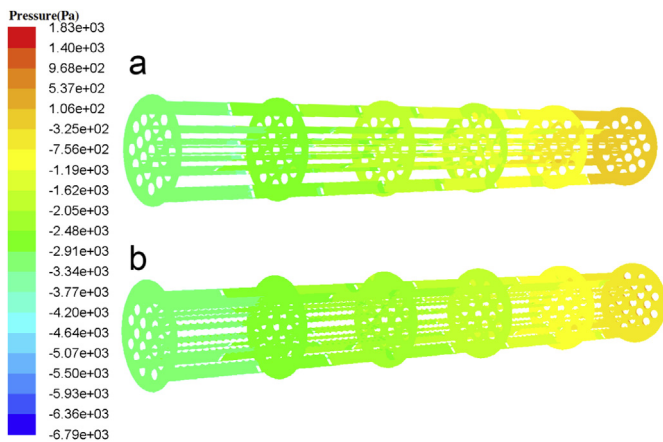


Fig. 11. The plots of pressure fields in different heat exchangers. (a) The plots of pressure fields in RBHX. (b) The plots of pressure fields in RBHXsSCT with one-start spirally corrugated tubes.

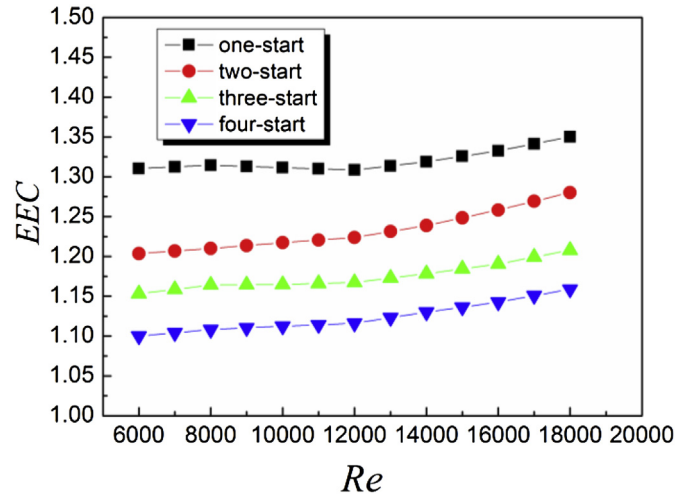


Fig. 12. EEC values of RBHXsSCT on various Reynolds number.

The result shows that the direction of velocity  $\vec{U}$  deviates more greatly from the direction of pressure gradient  $\nabla p$ . Therefore, the synergy between vectors  $\vec{U}$  and  $\nabla p$  should be minimized to design low-resistance heat exchangers.

#### 4. Conclusion

The numerical analysis of heat transfer and fluid flows in the shell sides of the RBHXsSCT and RBHX is carried out, with the aim to improve the overall thermo-hydraulic performance in longitudinal flow heat exchangers. The major findings are summarized as follows:

The velocity vector plots show that in RBHX, the vortices are generated when the fluid flows across the rods. However, in RBHXsSCT, little vortices are generated and the fluid is led by the spiral flow channels to flow against the tube walls. The different flow structures between the RBHXsSCT and RBHX result in different thermo-hydraulic performance in these heat exchangers.

The numerical results show that the Nusselt number in RBHXsSCT with one-start spirally corrugated tubes can be 1.2 times than that in RBHX when the Reynolds number is 18,000. The heat transfer quantities in the RBHXsSCT with one-start, two-start, three-start, and four-start spirally corrugated tubes are 104.6%,

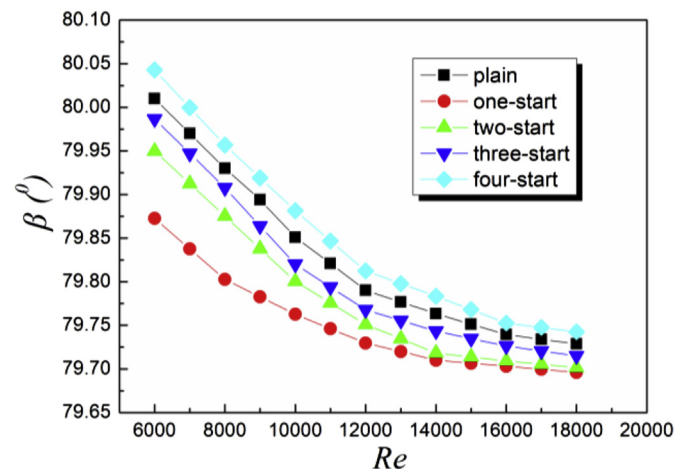


Fig. 13. The  $\beta$  of RBHXsSCT on various Reynolds number.

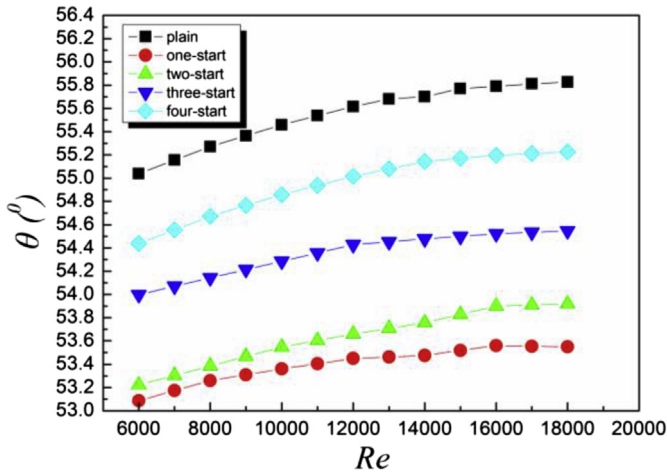


Fig. 14. The  $\theta$  of RBHXsSCT on various Reynolds number.

105.4%, 106.7%, and 109.6%, respectively, higher than that in RBHX. The pressure drop in RBHX is 1.21, 1.16, 1.12, and 1.08 times than that in RBHXsSCT with one-start, two-start, three-start, and four-start spirally corrugated tubes, respectively. The EEC value in RBHXsSCT with one-start spirally corrugated tubes can achieve 1.35, thereby making this heat exchanger promising to be widely applied in various industries.

The physical quantity synergy analysis is performed to investigate the heat transfer and flow resistance performance. The synergy angles  $\beta$  and  $\theta$  are calculated, and the results verify the synergy regulation among the physical quantities of fluid particles in the flow field of convective. The results of this study can guide us to design an optimum heat exchanger.

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### Nomenclature

$A_0$	the section area of the RBHX ( $\text{m}^2$ )
$A_s$	the section area of the RBHXsSCT ( $\text{m}^2$ )
$c_p$	the specific heat capacity ( $\text{kJ kg}^{-1} \text{K}^{-1}$ )
$C_{1e}$	empirical constant
$C_{2e}$	empirical constant
$C_{3e}$	empirical constant
$D$	the diameter of the shell side in heat exchanger (mm)
$D_e$	the equivalent diameter for shell side of the heat exchanger (mm)
$d_0$	the diameter of the plain tubes in RBHX (mm)
$d_r$	the diameter of the rod (mm)
$d_s$	the outer diameter of the spirally corrugated tubes in RBHXsSCT (mm)
EEC	the efficiency evaluation criteria
$G_b$	producing item of $k$ by buoyancy ( $\text{kg m}^{-1} \text{s}^{-3}$ )
$G_k$	producing item of $k$ by average velocity gradient ( $\text{kg m}^{-1} \text{s}^{-3}$ )
$h$	heat transfer coefficient ( $\text{W m}^{-2} \text{K}^{-1}$ )
$k$	turbulent kinetic energy ( $\text{m}^2 \text{s}^{-2}$ )
$M$	the mass flux ( $\text{kg s}^{-1}$ )
Nu	the Nusselt number
$n$	tubes numbers

$\Delta p$	shell side pressure drop (Pa)
$p_r$	rod diameter (mm)
$P$	power consumption in shell side (J)
$Q$	the heat transfer quantities in heat exchanger (W)
$S$	the heat transfer area in heat exchanger ( $\text{m}^2$ )
$S_k$	user defined source term ( $\text{kg m}^{-1} \text{s}^{-3}$ )
$S_e$	user defined source term ( $\text{kg m}^{-1} \text{s}^{-4}$ )
$\Delta t_m$	logarithmic mean temperature difference (K)
$T$	fluid temperature (K)
$u$	fluid velocity in shell side ( $\text{m s}^{-1}$ )
$U$	fluid velocity vector in general control equation ( $\text{m s}^{-1}$ )
$v$	volume flow rate ( $\text{m}^3 \text{s}^{-1}$ )
$x$	coordinate axis
$y$	coordinate axis
$Y_M$	contribution term from turbulent pulse expansion ( $\text{kg m}^{-1} \text{s}^{-3}$ )
$z$	coordinate axis

### Greek symbols

$\beta$	synergy angle ( $^\circ$ )
$\theta$	synergy angle ( $^\circ$ )
$\lambda$	thermal conductivity ( $\text{W m}^{-1} \text{K}^{-1}$ )
$\rho$	fluid density ( $\text{kg m}^{-3}$ )
$\phi$	universal variable (-)
$\Gamma$	generalized diffusion coefficient (-)
$\epsilon$	turbulent dissipation rate ( $\text{m}^2 \text{s}^{-3}$ )
$\mu$	dynamic viscosity ( $\text{kg m}^{-1} \text{s}^{-1}$ )
$\sigma_k$	Prandtl numbers corresponded to $k$
$\sigma_\epsilon$	Prandtl numbers corresponded to $\epsilon$

### subscripts

$i, j$	tensor
in	inlet water
$k$	kinetic energy term
0	RBHX
out	outlet water
$s$	RBHXsSCT
sct	spirally corrugated tubes

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