Optimization design of slotted fins based on exergy destruction minimization coupled with optimization algorithm

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- Genetic algorithm
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ABSTRACT

In this paper, the influence of the slot parameters of the slotted fins on the flow and heat transfer performance and the exergy destruction are studied by numerical simulation, and the optimal parameters corresponding to the best overall performance and the minimum exergy destruction are obtained by the method of CFD coupled with optimization algorithm, respectively. In current work, the slot length and width are taken as parameters (slot length 1.2–2.1 mm, slot width 0.1–1.0 mm), 100 different cases are studied under the same boundary conditions, and the results are analyzed and optimized by the neural network and genetic algorithm. The overall performance is taken as the evaluation of the heat transfer performance and the power consumption, while exergy destruction caused by heat transfer and fluid flow are taken as the estimate of the loss of available energy and mechanical work. The results show that the overall performance is best when the slot length and width are 1.38 mm and 0.27 mm respectively, and the overall performance is 13.1% higher than that of flat fin. While the exergy destruction caused by heat transfer and fluid flow are minimized synergistically when the slot length and width are 1.37 mm and 0.12 mm, and the irreversible loss caused by heat transfer is reduced by 19.13%, at the cost of an increase of 40.6% in the irreversible loss caused by fluid flow. The difference between the parameters corresponding to best overall performance and exergy destruction minimization means the irreversible loss of heat transfer and fluid flow process is not minimum when the overall performance is best, and indicates the exergy destruction minimization can be a principle to evaluate the heat transfer and flow process. The result in this paper is of great significant to the energy utilization and the improvement of the thermal quality in waste heat recovery.

1. Introduction

Finned tube heat exchangers are widely used in power, chemical, petrochemical and refrigeration engineering. It is meaningful to improve the heat transfer performance of the finned tube heat exchangers to save the energy consumption and the economic costs. The thermal resistance of the heat transfer process in the fin tube bundles consists of three parts: convective heat transfer resistance on the air side, conductive thermal resistance of the metal wall and the convective heat transfer resistance on the liquid side inner the tube [1,2]. The thermal resistance on the air side is the largest because of the low thermal conductivity of the air, so the key to improving the performance of the heat exchangers is to enhance the heat transfer and fluid flow performance in the air side [3,4]. Compared to the flat fin surface, the use of enhanced fin surface can greatly improve the heat transfer performance and it is the most effectively way to reduce the thermal resistance in the air side [5,6]. There are already many enhanced surfaces developed, such as slotted fin, louver fin, wavy fin and vortex generators [8]. And the enhanced surfaces can effectively increase the surface area, disturb the fluid flow [9] and prevent the development of boundary layer, at the same time, it leads to greater pressure loss. Among all of the enhanced surfaces, the slotted fins are more attractive to many researchers because of their simple geometric structure, good heat transfer enhancement with relatively low pressure drop [10,11]. The performance of slotted fin tube heat exchangers is related to many parameters [12], and the geometric parameters independent of the fin surface including tube pitch [13,14], fin thickness and fin pitch [15] and so on. However, when the space of the heat exchanger is fixed, it is very
difficult to further improve the performance by optimizing these parameters. So many researchers have studied the effects of slot parameters of the slotted fins on the performance improvement of the heat exchangers. The study shows that the performance of continuous slotted fins is higher than that of the alternating slotted fins [16]. Different types of slots can generate different types of vortexes and thus have different performance [17], because the intensity of the secondary flow on the fin surface determines the flow heat transfer characteristics of the slotted fin tube heat exchangers [18]. From the perspective of the nature of heat transfer enhancement, the filed synergy principle [19–21] are adopted to analyze the changes of the filed synergy angle, and the analysis results shows that the influence of various parameters on the overall performance can be well described and explained by the synergy principle [22–24].

However, the studies mentioned above mainly focus on increasing the heat transfer, which is based on the first law of thermodynamics, and only the temperature or the heat flux are considered. From the perspective of the second law of thermodynamics, not only the quantity in the heat transfer, but also the quality should be considered. Therefore, for the heat transfer and fluid flow in the finned tube heat exchangers, the heat transfer should be enhanced and the irreversible loss of the heat transfer process as well as the power consumption should be reduced. And the new alternative criterions based on the second thermodynamics are proposed to guide the optimization of flow and heat transfer, such as entropy generation minimization [25,26], entransy [27], available potential [28] and the expression of local exergy destruction derived from the equation of available potential. Different from entransy or entransy dissipation, the local exergy destruction is not only suitable for evaluating the irreversibility of heat transfer process, but also for the fluid flow, and the exergy destruction caused by fluid flow are proposed [28]. The exergy destruction caused by heat transfer represents the loss of the available energy, while the exergy destruction caused by flow fluid represents the power consumption and it fully represents the loss of mechanical work. The research demonstrated the approach of exergy destruction minimization is an effective way to optimize the convective heat transfer and it differs from the approach which taking the overall performance as the objective [29]. Moreover, the exergy efficiency is an effective evaluation criterion for convective heat transfer [30]. In order to develop a new method to guide the heat transfer optimization, it is necessary to analyze the distribution of the temperature in the whole filed, which is of great significance in practical engineering.

Due to the complexity of the geometry of the slotted fins, it is difficult to adopt the traditional optimization design method to find the optimal geometric parameter configuration, which is mainly based on empirical chosen and the results of predecessors [31] and could only find the local optimal solution. Therefore, during the design of the finned tube heat exchanger, it is necessary to find the global optimal solution by the optimization algorithm [32,33]. Recently, some studies have applied genetic algorithm (GA) to heat transfer optimization of fined tube heat exchangers [34–36], and found that the GA can get the global optimal solutions within a limited range [37–40]. While the artificial neural network (ANN) can make a good prediction of the unknown results based on the existing results, which greatly saves the computational costs [41–43]. And the key to obtaining a suitable ANN is to get the appropriate activation function and training function by training the data set.

As mentioned above, in the published literature, they mainly studied the slotted fin geometry parameters based on the first law of thermodynamics, and little research studied the effect of the slot size on the performance of slotted fins. So, in this paper, both from the perspective of the first law of thermodynamics and second law of thermodynamics, the effects of the slot length and width on the fin performance are studied. In order to achieve the best performance of the heat exchangers, the overall performance and exergy destruction are taken as optimization objective respectively, and the optimization algorithm is used to find the optimal slot parameters.

2. Numerical simulation

2.1. Physical model

The flat and slotted fin tube bundles are shown in Fig. 1, and the four tubes are arranged staggered along the flow direction. Except some slotted blocks on the slotted fin surface, which are continuously

![Fig. 1. Physical model of the fin tube bundles (a) flat fin (b) slotted fin.](image-url)
The detailed parameters of the fin tube bundles are configured, as shown in Fig. 1(b), the parameters of slotted fin surface are the same as that of flat fin, such as the fin thickness, the fin pitch and tube pitch and so on. The detailed parameters of the fin tube bundles are listed in Table 1.

The regions enclosed by the dotted line shown in Fig. 1 is selected as computational domain, the computational domains of flat and slotted fins as well as the boundary conditions are shown in Fig. 2. The central domain, while the upper and lower domain are the gas domains that part of the computational domain along the Z direction is the solid fin surround the solid fins, which is clearly shown in Fig. 2(a). The upper and lower surfaces are set as periodic boundaries; while the left and right surfaces are set as symmetry boundaries. The velocity of gas at the inlet dissipation requirements under fixed heat loads, so the heat flux of the wall is considered as constant and the heat flux is 19436 W/m².

The effect of turbulence on the fluid flow is included by applying the k – ε model. As for the physical properties of the air, firstly the physical properties are obtained at the inlet temperature $T_{in}$ and the outlet temperature $T_{out}$ is known after the numerical simulation, and then the physical properties are obtained at the mean temperature $\left(T_{in} + T_{out}\right)$, then the second simulation is carried out and a new $T_{out}$ is obtained. Due to the difference between the air physical properties obtained at the mean temperature $\left(T_{in} + T_{out}\right)$ and $\left(T_{in} + T_{out}\right)/2$ is negligible, so the physical properties of air are obtained at the mean temperature $\left(T_{in} + T_{out}\right)/2$ in the following simulation, which is 329.5°C. The $T_{in}$ and $T_{out}$ are the temperature of air at inlet and outlet, respectively. The coupling of pressure and velocity is solved by SIMPLE algorithm, and the convergence criteria of the continuity, momentum and energy are $10^{-4}$, $10^{-6}$ and $10^{-8}$, respectively.

The distributions of temperature and pressure throughout the flow field is non-uniform, and the temperature at each point on the surface is different, so the mass weighted average method is adopted to obtain the average temperature and pressure at the inlet and outlet. The average temperature and pressure of the gas are defined as follows:

$$T = \frac{\int \rho u T \, dA}{\int \rho u \, dA}$$  \hspace{1cm} (4.1)

$$p = \frac{\int \rho u^2 p \, dA}{\int \rho u \, dA}$$  \hspace{1cm} (4.2)

In order to better describe the results, some dimensionless parameters for evaluating the performance of the finned tube bundles are defined. The Reynolds number and friction factor are defined as follows:

$$Re = \frac{\rho u_{rms} D_h}{\mu}$$  \hspace{1cm} (5)

$$f = \frac{\Delta p}{0.5 \rho u_{rms}^2}$$  \hspace{1cm} (6)

The $u_{rms}$ is the velocity at the minimum flow area, $\Delta p$ is the pressure drop between inlet and outlet, $\Delta p = p_{in} - p_{out}$.

The Nusselt number is defined as:

$$Nu = \frac{h D_h}{\lambda}$$  \hspace{1cm} (7)

$$D_h = \frac{4 A_t L_{in}}{A_s}$$  \hspace{1cm} (8)

where $h$ is the average heat transfer coefficient, defined as:

$$h = \frac{Q}{\Delta T A}$$  \hspace{1cm} (9)

$Q$ is the total heat flux rate, calculated by the expression:

$$Q = \dot{m} C_p (T_{in} - T_{out})$$  \hspace{1cm} (9.1)

and $\Delta T$ is the logarithmic mean temperature difference, calculated by the expression:

$$\Delta T = \frac{(T_{in} - T_{out}) - (T_{in} - T_{out})}{\ln (T_{in} - T_{out}) / (T_{in} - T_{out})}$$  \hspace{1cm} (9.2)

In order to better compare the overall performance between finned tube bundles with different parameters, a dimensionless evaluation index $j_e$ is defined, and the expression of $j_e$ is given below:

$$j_e = \frac{Nu / f_0}{\left(f_0 / f_0\right)^{1/3}}$$  \hspace{1cm} (10)

where $Nu_0$ and $f_0$ is the Nusselt number and friction factor of the flat fin, the larger $j_e$ is, the better the overall performance of the finned tube bundles is.

### Table 1

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fin thickness (δ/mm)</td>
<td>0.3 0.3</td>
</tr>
<tr>
<td>Fin pitch (mm)</td>
<td>2 2</td>
</tr>
<tr>
<td>Slot pitch (mm)</td>
<td>1 1</td>
</tr>
<tr>
<td>Diameter of tube (D/mm)</td>
<td>8 8</td>
</tr>
<tr>
<td>Transverse tube pitch (S/mm)</td>
<td>6.6 6.6</td>
</tr>
<tr>
<td>Longitudinal tube pitch (S/mm)</td>
<td>21 21</td>
</tr>
<tr>
<td>Length of the fin (Lfin mm)</td>
<td>80 80</td>
</tr>
<tr>
<td>Length of the inlet section (mm)</td>
<td>80 80</td>
</tr>
<tr>
<td>Length of the outlet section (mm)</td>
<td>260 260</td>
</tr>
<tr>
<td>Material</td>
<td>Aluminum Aluminum</td>
</tr>
<tr>
<td>Length of slots (L/mm)</td>
<td>1.2–2.1 /</td>
</tr>
<tr>
<td>Width of slots (W/mm)</td>
<td>0.1–1.0 /</td>
</tr>
<tr>
<td>Height of strips (H/mm)</td>
<td>2.25 /</td>
</tr>
</tbody>
</table>

Due to the temperature difference is not significant in the whole field, and the energy equation:

$$\frac{\partial \left(\rho u T\right)}{\partial x_i} = 0$$  \hspace{1cm} (1)

and momentum equations:

$$\frac{\partial}{\partial x_i} \left(\rho u \frac{\partial u_i}{\partial x_i}\right) = \frac{\partial}{\partial x_i} \left(\frac{\mu}{\rho} \frac{\partial u_i}{\partial x_i}\right) = \frac{\partial p}{\partial x_i}$$  \hspace{1cm} (2)

and the energy equation:

$$\frac{\partial}{\partial x_i} \left(\rho u_i T\right) = \frac{\partial}{\partial x_i} \left(\frac{1}{C_p} \frac{\partial T}{\partial x_i}\right)$$  \hspace{1cm} (3)

where $\lambda$ is thermal conductivity of the air, and $C_p$ is the specific heat capacity of the air.

2.2. Governing equations and parameter definition

Numerical simulation approach is used to study the three-dimensional steady, turbulent flow and heat transfer characteristics on the fin surfaces, and the coupling between fluid and solid is considered. Due to the temperature difference is not significant in the whole filed, the air is considered as incompressible fluid with constant physical properties. The governing equations to be solved include continuity, momentum and energy equations, they are given in the following forms: continuity equation:

$$\frac{\partial \left(\rho u_i\right)}{\partial x_i} = 0$$  \hspace{1cm} (1)

and momentum equations:

$$\frac{\partial}{\partial x_i} \left(\rho u_i u_j\right) = \frac{\partial}{\partial x_i} \left(\frac{\mu}{\rho} \Delta u_i\Delta x_i\right) = \frac{\partial p}{\partial x_i}$$  \hspace{1cm} (2)

and the energy equation:

$$\frac{\partial}{\partial x_i} \left(\rho u_i T\right) = \frac{\partial}{\partial x_i} \left(\frac{1}{C_p} \frac{\partial T}{\partial x_i}\right)$$  \hspace{1cm} (3)

where $\lambda$ is thermal conductivity of the air, and $C_p$ is the specific heat capacity of the air.
As mentioned above, the irreversibility must be taken into account, so to quantitatively evaluate the irreversibility of the flow and heat transfer process, the local exergy destruction caused by heat transfer are introduced below [28]:

\[ i_o = T_0 \frac{\lambda (\nabla T)^2}{T^2} \]  \hspace{1cm} (11)

where \( T_0 \) is the ambient temperature, and the total exergy destruction in the flow region is obtained by integration \( I_0 = \iiint i_o dV \). Meanwhile, the local exergy destruction caused by fluid flow [28]:

\[ i_1 = u \cdot \nabla p \]  \hspace{1cm} (12)

the total exergy destruction caused by fluid flow in the flow region is obtained by integration \( I_1 = \iiint i_1 dV \). The exergy destruction caused by fluid flow completely represents the loss of mechanical work, and the higher it is, the larger the power consumption is, so reducing the loss can help to reduce the flow power consumption. However, \( I_1 \) and \( I_0 \) are not independent, and the decrease of \( I_0 \) leads to the increase of \( I_1 \). So this
study aims to optimize the geometric parameters of the fin surface so that the two exergy destruction can achieve synergistic minimization.

2.3. Design of optimization algorithm model

There are 100 sets of results in this paper, and the results are processed by the optimization algorithm. Firstly, the artificial neural network (ANN) is applied to train the results [44], the structure of the ANN is shown in Fig. 3, there are two inputs, and one or two outputs according to the different objectives. Two kinds of evaluation criteria of the optimization design are considered: one is the overall performance based on the first law of thermodynamics and there is only one output $j_C$; the other is the exergy destruction minimization based on the second law of thermodynamics and there are two outputs, namely, exergy destruction caused by fluid flow $I_1$ and heat transfer $I_0$. With the well-trained ANN, the output results beyond the 100 sets of parameters can be well predicted [45], without calling the CFD software, and it is obviously that this approach saves much time and costs. By adjusting the training parameters of the neural network, the precision of the outputs can be precisely controlled [45], for the training data, the most deviation between the existing results and the predicting results is 6%, so the well-trained ANN is reliable.

The genetic algorithm (GA) is used to find the optimal solutions. The well-trained ANN is taken as the database of the GA, and the geometric parameters of the GA fitness function are entered to the database and then the results are retrieved from the database, the coupling between the ANN and the GA is shown in Fig. 4. The GA is an algorithm that simulates the biological evaluation to find the optimal solutions [46] after selection, crossover and mutation, namely, eliminate inferior individuals and produce next generation populations. The initial individuals are generated from the search space, and the fitness value are evaluated and assigned by the fitness function, and the fitness function is based on the objectives, the individuals with high fitness value have the chance to survive to the next generation. In this work, the search space of the slot width is ranging from 0.1 mm to 1.0 mm; and the slot length is ranging from 1.0 mm to 2.5 mm. After the optimization, the optimal overall performance and the minimum exergy destruction in the search space is obtained.

The overall performance and the exergy destruction are optimized separately as two different objectives, so two sets of neural network structures are used, as shown in Fig. 3. The input parameters of the two structures are both the slot length and the slot width, and for both of the structures, there are single hidden layers, single input layers and single output layers. For the optimization of single objective $j_C$, the TRAINLM function is adopted as the training function, and TANSIG function is adopted as the activation function, the initial population of the genetic algorithm is taken as 50, the generations of evolution are 50, the convergence criterion is $10^{-6}$. For the optimization of objectives $I_0$ and $I_1$, the TRAINBR function is adopted as the training function and the TANSIG function is adopted as the activation function, the initial population of the GA is 70, the evaluation generations are 1000, the
2.4. Grid independence and model validation

In order to avoid the impact of the grid numbers on the results, it is necessary to verify the independence of the grid numbers. The unstructured grids are used to generate the computational grids because the geometry of the slotted fin is complicated. Generally, the grids near the wall is refined, especially for the wall near the slot where the swirling flow exists, and the grids in the inlet and outlet sections are coarse to save the time and cost, the grid details near the extended and fin domains are shown in Fig. 5. The slotted fin with the slot length 2.1 mm and the width 1.0 mm is selected for the grid independence study, and the results are shown in Table 2. The results of the grids number 3806333 are selected as the reference, and it can be found that the deviation of the heat transfer coefficient of the grid number 2901137 and the grid number 3806333 is 0.235%, while the deviation of the $\Delta p$ is 0.44%. Therefore, the grid number 2901137 is used as the final computational grid number, and the maximum element size is 0.45 mm.

In order to verify the reliability of the numerical model, it is necessary to compare the computational results with the experimental data. The numerical simulation is carried out on the flat fins, the results are compared with experimental data [47] and simulation data [48]. As shown in Fig. 6, the results show well agreement of the Nusselt number $Nu$ and the pressure drop $\Delta p$ with the experimental data and the simulation data. Although the highest deviation of the $Nu$ is 8.31% when the $Re$ is 2399, the highest deviation of pressure $\Delta p$ is 13.88% when the $Re$ is 2399, the allowable deviation of the correlation is within 15%, so it is reasonable to believe the numerical model is reliable, and it is also acceptable in engineering application. Moreover, the deviation is highest when the $Re$ is 2399, this is because when $Re$ is small, the flow state is close to the transition zone from laminar flow to turbulent flow, the turbulence model is not suitable for this zone, so the deviation is large. But in the following studies, the $Re$ is far away from the transition zone.

Table 2

<table>
<thead>
<tr>
<th>Grids number</th>
<th>1701926</th>
<th>2279893</th>
<th>2901137</th>
<th>3806333</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heat transfer coefficient (W/m²⋅K)</td>
<td>37.6</td>
<td>38.3</td>
<td>38.5</td>
<td>38.6</td>
</tr>
<tr>
<td>Deviation (%)</td>
<td>2.00</td>
<td>0.55</td>
<td>0.235</td>
<td>/</td>
</tr>
<tr>
<td>$\Delta p$ (kPa)</td>
<td>1050.52</td>
<td>1066.42</td>
<td>1099.191</td>
<td>1094.37</td>
</tr>
<tr>
<td>Deviation (%)</td>
<td>4.01</td>
<td>2.55</td>
<td>-0.44</td>
<td>/</td>
</tr>
</tbody>
</table>

Fig. 5. Grid details near the extended and fin domains.

Fig. 6. Model validation of the numerical results (a) comparison of the $Nu$ (b) comparison of the pressure drop $\Delta p$. 
3. Results and discussion

3.1. The effects of the slot length and width on the overall performance

Fig. 7 compares the temperature on the fin surface for the flat fins and selected slotted fins (L = 2.1 mm and W = 0.5 mm), the enlarged views of the area enclosed by the dotted lines in Fig. 7(a) are shown in Fig. 7(b). It can be seen that on the most region of the slotted fin surface, the temperature is lower than that on the flat fin surface at the same location. And the high temperature region of the slotted fin surface is mainly concentrated on the end of the slotted fin surface, as shown in Fig. 7(b). This is because there is more heat on the fin surface taken away by the air, and the air temperature on the end of slotted fin surface is higher, so the temperature of the solid fin surface on the end is higher. Though there are small difference of the temperature on the fin surface, the temperature distributions on the fin surface are indeed changed, and the outlet temperature of the air is raised from 336.7 °C to 337.3 °C. So the slot can indeed improve the heat transfer performance, and the enhanced fin surface can disturb the fluid flow and prevent the development of the boundary layer, as discussed above. The velocity vector distribution of the flat fins and slotted fins are shown in Fig. 8, it can be found that there is large backflow region behind the tube wall of the flat fins, the flow and heat transfer performance in this area are very weak, and the heat transfer performance in the backflow region must be improved. The arrangements of slots can effectively reduce the backflow region, and the velocity distribution is uniform, and the flow field is more disordered, as shown in Fig. 8 (a). It is obviously that the velocity on the slotted fin surface is larger, the secondary flow is generated behind each slot, as shown in Fig. 8(b), the flow behind the slots is more disordered, so the impact of the fluid on the surface is stronger, the effect
of convective heat transfer is better, and more heat flux is taken away, the performance of the heat transfer is enhanced. However, the large velocity and the disordered distribution of the velocity vector also leads to larger pressure drop, which means the improvement of heat transfer is at the cost of the power consuming, it is detrimental in engineering applications. Considering the combined effects of the heat transfer and the pressure drop, the overall performance of the slotted fins and the flat fins must be compared.

Figs. 9 and 10 represent the heat transfer and fluid flow performance, it is clearly that the heat transfer performance of all slotted fins is better than that of flat fins; while the flow performance of the slotted fins is worse than that of flat fins, the pressure drop is larger at the same Re number. As shown in Figs. 9(a) and 10(a), the $Nu$ and friction factor vary in the same trend at different slot widths, $Nu$ increases first and then decreases as the slot length increases, and the friction factor $f$ increases linearly as the slot length increases. This is because when the slot length is short, the slot can well disturb the fluid flow, and destroy the boundary layer, which can effectively enhance heat transfer but cause a larger pressure drop. While with the further increase of the slot length, the slot is so long that leading to poor thermal conductivity of the metal.
fins, so the heat transfer performance of the slotted fin becomes poor; as for the friction factor, the longer slot length leads to smaller cross-section area, and the flow resistance as well as the pressure drop is greater, so the friction factor is larger. It can be seen from Fig. 9(b), when the slot length is shorter than 1.5 mm, the Nu increases first and then decreases as the slot width increases; while when the slot length is between 1.5 mm and 2.1 mm, the Nu decreases as the slot width increases. This is because when slot length is shorter than 1.5 mm, the size of the slot is small, and the increase of the slot width can enhance the disturbance of fluid flow, reduce the thermal boundary layer and improve the heat transfer performance. Nevertheless, when the slot length is longer, the size of the slot is large and the increase of slot width leads to larger slot size, which causes poor thermal conductivity of the metal fins. The friction factor varies little with the increase of the slot width, as shown in Fig. 10(b), because the increases of slot width can slightly affect fluid flow.

Fig. 11 shows the overall performances of the slotted fins varying with the slot length and slot width, the performance of the flat fins is as the reference. Firstly, it can be found that the performance of some slotted fins is worse than that of the flat fins, while the performance of most slotted fins is better than that of the flat fins. The slots on the fin surface increase the heat transfer and the flow resistance at the same time, when the heat transfer enhancement is less than the cost of the increase of the flow resistance, the performance of the slotted fins is inferior to that of flat fins. Also it can be seen from Fig. 11 (a) that, for the different slot widths, the influence of the slot length on the overall performance is the same: with the increase of the slot lengths, the index $j_C$ increases at first, and then decreases, moreover, with the further increase of the slot length, the $j_C$ is lower than 1. While the influence of slot width on the overall performance depends on the slot length: when the slot length is small, with the increase of the widths, the index $j_C$ increases first and then decreases; when the slot length increases, the increasing trend of the index $j_C$ becomes weak, and when the slot length is larger than 1.5 mm, the index $j_C$ decrease as the slot width W increases, as shown in Fig. 11 (b). So in the range of the parameters studied, there must exist a set of slot length and width to achieve the best overall
Since the simulation error exists, some points on the graph fluctuate up and down, the graph is not very smooth, but the trend of all graphs is the same, so the above conclusion is reliable.

Based on the analysis above, the 100 sets of data of the overall performance is taken as the training database for the neural network, and the index $j_c$ is adopted as the fitness for the GA to optimize and predict the results. The optimization tracing figure of GA based on the fitness $j_c$ is shown in Fig. 12. It can be seen that after 37 generations, the average fitness consistent with the best fitness, the globally optimal parameters of slot length and width are solved, and the best fitness are achieved. The best overall performance given by the optimization is 1.131, and the slot length and width are $L = 1.38$ mm and $W = 0.27$ mm, respectively. This set of slot parameters is taken as the geometric parameters to build the physical model and the numerical simulation is carried out to verify the performance, the numerical result of the overall performance is 1.1268. The difference between the numerical result and the optimization result is less than 1%, so the accuracy of the optimization algorithm is believable and the parameters are recommended to get the best overall performance.

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**Fig. 11.** (a) Overall performance at different slot lengths (b) Overall performance at different slot widths.

**Fig. 12.** The optimization tracing figures of GA based on fitness function $j_c$.

**Fig. 13.** The exergy destruction caused by the heat transfer (a) varies with the slot length (b) varies with the slot width.
3.2. The effects of the slot length and width on the exergy destruction

Fig. 13 and Fig. 14 represent the variation of the exergy destruction caused by the heat transfer and fluid flow. The exergy destruction caused by heat transfer represents the loss of the available energy. It can be found from Fig. 13 that with the increase of the slot length, the exergy destruction caused by transfer decreases first and then increases, and the smaller the slot width is, the more obvious this trend is, as shown in Fig. 13(a); while the variation of the heat transfer exergy destruction with the slot width depends on the length, when the slot length is small, the exergy destruction decreases first and then increases with the increase of the width, and when the slot length is greater than 1.5 mm, the exergy destruction decreases as the slot width increases, as shown in Fig. 13 (b). The variation of the exergy destruction with the slot parameters is related to the influence of the slot parameters on the temperature filed, namely, when the temperature gradient is decreased, the value of equation (11) is small and the exergy destruction is small. While the exergy destruction caused by the fluid flow totally represents the loss of the mechanical work, and it is directly related to the pressure drop. The exergy destruction caused by fluid flow is different from the exergy destruction caused by heat transfer, it increases almost linearly with the increase of the slot length, as shown in Fig. 14(a), while it increases slightly as the slot widths increase, as shown in Fig. 14 (b). This is because the increase of the slot length will reduce the flow cross-section area, which leads to the increase of the flow resistance, as a result, the loss of the mechanical work increases, and the exergy destruction increases as the slot length increases. And the increase of the slot width will increase the contact area between the fluids and solid, so the heat transfer performance and the mechanical work both increase, as shown in Figs. 13 (b) and 14 (b).

As discussed above, the exergy destruction represents the loss of available energy and mechanical work, so reducing the exergy destruction can improve the thermal quality of the gas, reduce the flow resistance and the power consumption [28]. On the one hand, in order to reduce the temperature gradient, obtain the uniform temperature field, it is necessary to minimize the exergy destruction caused by the heat transfer; on the other hand, the improvement of heat transfer inevitably leads to an increase in power consumption, in order to minimum the increase in power consumption and flow resistance, it is necessary to minimize the exergy destruction caused by the fluid flow, so $I_0$ and $I_1$ are chosen as the optimization objective. The ultimate purpose is to minimize the two exergy destruction, and the pareto front given by the optimization algorithm is shown in Fig. 15, a series of optimization solutions are given by the GA, and the best solution is found by The Topsis methods: the minimum exergy destruction caused by heat transfer is 13305.3 W, the minimum exergy destruction caused by fluid flow is 4652.142 W, as marked in Fig. 15, the corresponding slot length and width are 1.37 mm, 0.12 mm, respectively. This set of slot parameters is taken as the geometric parameters to build the physical model and the numerical simulation is carried out to verify the optimal results, the numerical results show that the $I_0$ and $I_1$ are 12948.7 W and 4595.9 W, respectively, the difference between them are under 2.69% and 1.21%, so the best solution is reliable and the slot parameters are recommended to obtain the minimum exergy destruction.

4. Conclusion

In this paper, the numerical simulation is carried out to study the influence of the slot parameters on the overall performance and the exergy destruction, the main findings are as follows:

1. The heat transfer performance of the slotted fins is better than that of the flat fins because of the enhanced surface geometry, while only the slotted fins with appropriate slot parameters have the better overall performance than the flat fins.
2. The effects of the slot length on the overall performance and the exergy destruction are great, while the effects of the slot width are slight. And there exist optimal solution of the overall performance and exergy destruction in the range of the slot parameters studied.

3. The overall performance is best when the slot length and width are 1.38 mm and 0.27 mm respectively, and the overall performance is 13.1% higher than that of flat fin.

4. The exergy destruction caused by heat transfer and fluid flow are minimized synergistically when the slot length and width are 1.37 mm and 0.12 mm, and the irreversible loss caused by heat transfer is reduced by 19.13% with the cost of an irreversibility increase of 40.6% caused by fluid flow.

5. The difference between the two evaluation criteria proves that the best overall performance does not correspond to the minimum loss of the available energy and the mechanical work, which means the exergy destruction minimization also can be a principle to guide the heat transfer enhancement. The improvement of the thermal quality of the air in the outlet is significant and beneficial to improve the energy efficiency.

**Declaration of competing interest**

The authors claim that none of the material in the paper has been published or is under consideration for publication elsewhere.

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**Appendix A. Supplementary data**

Supplementary data to this article can be found online at https://doi.org/10.1016/j.ijthermalsci.2019.106133.

**Nomenclature**

\[ A \] Flow area \((m^2)\)

\[ A_c \] Minimum flow area \((m^2)\)

\[ A_0 \] Total surface area \((m^2)\)

\[ C_p \] Specific heat capacity of air \((J/kg\cdot K)\)

\[ D \] Diameter of the tube \((mm)\)

\[ D_h \] Hydraulic diameter \((mm)\)

\[ H \] Height of the strips \((mm)\)

\[ L_{fin} \] Length of the fin \((mm)\)

\[ L \] Slot length \((mm)\)

\[ p \] Pressure \((Pa)\)

\[ T \] Fluid temperature \((K)\)

\[ u_{i} \] Velocity \((m/s)\)

\[ u_{amin} \] Velocity at the minimum flow area \((m/s)\)

\[ W \] Slot width \((mm)\)

\[ S_t \] Transverse tube pitch \((mm)\)

\[ S_l \] Longitudinal tube pitch \((mm)\)

\[ \delta \] Fin thickness \((mm)\)

\[ \rho \] Fluid density \((kg/m^3)\)

\[ Q \] Total heat flux rate \((W)\)

\[ m \] Mass flow rate of air \((kg/s)\)

\[ \mu \] Dynamic viscosity \((Pa\cdot s)\)

\[ \lambda \] Thermal conductivity of air \((W/m\cdot K)\)

\[ I_0 \] Exergy caused by heat transfer \((W)\)

\[ I_1 \] Exergy caused by fluid flow \((W)\)

\[ j \] Index of overall performance

\[ \nabla \] Gradient

**References**


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